

IMAGE COMPRESSION USING DISCRETE TCHEBICHEF TRANSFORM AND SINGULAR VALUE DECOMPOSITION (DTT-SVD)

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Abstract:

Nowadays, images are sent through the internet in very large scale. More memory space and transmission bandwidth are needed for an uncompressed image. So, it increases the size of the image database. By greatly reducing the need for bit-rate by using the redundancies that are usually present in video and image signals, compression can be accomplished. The device that achieves a high degree of compression while retaining information relevant to the sensitive pictures is necessary. The DTT will replace the DCT. The new high-energy compaction and lower transformation of computational benefit used for compression are DTT. A given matrix is divided into a product of orthonormal matrices and a diagonal matrix by the SVD technique. Combining the DTT and SVD strategies speeds up the transition of the image into a non-visual format intended to minimise inter-pixel redundancy, and without compromising efficiency, the SVD will delete enormous portions of our matrix. DTT-SVD compression has been shown to result in higher CR, PSNR values ranging from 28 to 32db, and lower MSE values compared to the DCT and SVD form combine (DCT-SVD).

Keywords: Image compression, Discrete Cosine Transform, Discrete Tchebichef Transform, Singular Value Decomposition, MSE, PSNR.

1. Introduction

The primary objective of image compression systems is to reduce the memory needed to store the images and to transfer the images over longer distances at minimum expense and time. Researchers have developed powerful image compression techniques over the last couple of decades to increase the compression rates and the accuracy of images. In various signal processing

applications, several efficient transforms such as DCT (Discrete Cosine Transform), KLT (Karhunen-Loeve Transform), WT (Wavelet Transform), and QFT (Quick Fourier Transform), were advanced and used significantly over the era. In image compression, image processing techniques which use orthogonal-kernel functions are commonly used. DCT (Discrete Cosine Transform), which is used in the JPEG compression standard, is one of the generally known image transfer methods[1]. DTT is the genre of orthonormal orthogonal conversion (Discrete Tchebichef Transform). It is built from a different class of common Tchebichef polynomials and has image analysis and compression applications [2-9]. An orthonormal variant of Tchebichef moments has been established and many computational characteristics have been analyzed [10]. Mukundan and Hunt [11] have shown that DTT and DCT for natural images demonstrate nearly equal energy compactness. The Tchebichef transformation is generally a better transformation than the DCT, since the sampling points can be chosen to be non-equidistant as they converge faster. DTT can also be used instead of DCT [12]. In transform-based techniques, only a few coefficients or pixels are chosen to transmit or store the images. These techniques can be further extended with singular value decomposition (SVD) and use the resemblance of the local pixels of an image to minimise the data size of large images. Compression is accomplished in SVD by taking the rank of a matrix down to almost the original matrix to represent an image in large images with the exploitation of higher similarity between local pixel groups. In this article, an effective compression and reconstruction technique with a combination of DTT and SVD was proposed to test its output estimation in an image.

2. Review of Literature

2.1. Compression using DCT

One of the best methods of transformation used in the JPEG compression process is DCT. To eliminate and extract redundancies in the image using different transformation algorithms, several researchers have put forward image compression schemes. Since several methods of transformation have already been developed and used in the compression field, researchers are now trying to adopt a new method of transformation known as Discrete Tchebichef Transformation (DTT). It is compact with high energy, cost-effective in space, and has better performance than the DCT. Many researchers who have tried to compress images using DTT have given legitimate explanations and recommendations for the use of the DTT approach of image compression. For example, due to its simplicity and high energy compaction, Pennebaker et al.[1] proposed that DTT could be used as an alternative to DCT. It is one of the picture transformation techniques in image compression using orthogonal kernel functions. An study based on the transformation of the Discrete Tchebichef Polynomial on the orthogonal moment function was performed by Mukundan et al.[3] and found that it is superior to the moments of Legendre and Zernike and that they are also considered to be the basis for the transformation of the polynomial and cosine of Chebyshev.

2.2. Compression using DTT

In their research based on DTT, Ishwar, et al.[4] A quick 4X4 algorithm computation and its image implementation indicated that the DTT architecture is strong compared to the DCT architecture. Then, Abdelwahab[6] suggested a low-complexity multiplication free Discrete Tchebichef Transform approximation. For their proposed approximation, a minimal number of additions and bit-shifting operations are needed. Dynamic power consumption and area are reduced relative to the new DTT approximation architecture. Senapati et al.[20] have shown that DTT's characteristics are not the same as DCT's characteristics, since DTT also has high energy compactness and low computational benefits. Via the tests, they showed that DTT requires a lower number of bits to encode the coefficients than DCT. Using the Tchebichef psychovisual threshold, Ernawan et al.[21] developed a strategy for image compression to generate an optimum bits-budget of image signals in which the bits-budget is constructed to eliminate the primary function of image compression quantification tables. It is proven that 42 percent of JPEG compression will increase the visual efficiency of the image output by the suggested bit

budget technique. A study on the use of compression techniques in the cache and main memory structures was performed by Mittal and Vetter (2016). As a result of their survey, it is known that CPUs, GPUs, non-volatile memory systems, 2D and 3D memory systems have multiple forms of compression. In addition, Fouzi Douak [23] used optimization techniques to implement an innovative dictionary architecture based on DCT and DTT, and compared the performance of DCT and DTT based dictionaries. Finally, it has been seen that the DTT-based dictionary is more reliable than the DCT dictionary.

2.3. Compression using SVD

Similarly, the use of Singular Value Decomposition (SVD) techniques is another advance of image compression. The efficiency of image compression techniques based on SVD was also researched and investigated by Brady Mathews [18]. During the process, SVD splits a matrix into three essential sub-matrices to represent the data. Matrix A, for instance, where A can be divided into three sub-matrices $A = U\Sigma V^T$. Then, there is another suggestion made by Swathi H R et al[19] with advanced features to achieve image compression. In this analysis, they proposed that any random, square, reversible, and non-reversible matrix of the M X N size could be adapted to the SVD. Mean Square Error and Compression Ratio are used as performance metrics. Candès et al[24] then suggested that the process of matrix completion has two major restrictions. Firstly, the matrix to be settled should be thin, and secondly, as opposed to its proportions, the matrix to be reconstructed should be inferior. A hybrid KLT-SVD system was proposed by Wadem P et al. [25]. KLT stands for Converting Karhunen-Lobve. A picture holds statistical anomalies that are local to the image. They exploited this fact and the use of adaptive switching strategies to convert image coding. Similarities between SVD and KLT were noticed. This technique is often used to increase the performance of coding, from Prasantha H.S. et al.[26] Singular value decomposition on the image matrix has been introduced to achieve compression of the image. For each picture, the matrix is set up and the graph plotted as per points for different ranks. Furthermore, it is noted that as the rank in the image matrix increases, the number of appearances will also increase, contributing to a related change in the image quality. Because of this smaller ranks have obtained a larger compression ratio

3. Proposed work

Images can be compressed by eliminating redundant information. First, an image is subdivided by N*N image block and it is transformed into image signals using Tchebichef transform. The method consists of a doubly nested loop. Each variables x and y go through from 0 up to N-1. In addition, the inner sum requires (N-1) additions and the outer sum requires (N-1) additions of the inner sums. Therefore, it requires (N-1)N+(N-1) = (N-1)(N+1) additions.

In addition, for each product word, two multiplications are necessary, so the number of multiplications needed for computing T_{pq} is $2N^2$. T_{pq} needs to be computed for p, q = 0...N-1. Therefore, $2N^2$ and $N^2(N-1)(N+1)$ respectively are the cumulative number of multiplications and additions required to compute all the transformed coefficients. Tchebichef Moment has more AC coefficients and on each picture block there is just one DC coefficient. The DC coefficient is encoded by a 24-bit number as the fundamental colour of the block. The quantization function is substituted by DTT.

An image is a matrix, whose elements are in numbers, and they are the intensity values of the corresponding pixels in an image. The decomposition procedure of singular value is then used to decompose the matrix into three matrices.

$$A = (U_1, U_2, \dots, U_n) \begin{pmatrix} \sigma_1 & \dots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \dots & \sigma_n \end{pmatrix} \begin{pmatrix} V_1^T \\ \vdots \\ V_n^T \end{pmatrix} \tag{1}$$

Find eigenvalues of the image matrix. Obtain singular values (square root of eigenvalues). Place singular values in diminishing order as a diagonal matrix, S matrix using image matrix, say A, obtain AA^T and $A^T A$. Find the eigenvector of above matrices. These vectors become rows and columns of V and U matrices. Now, matrix A can be portrayed by using S, U, and V matrices. Consequently, efficient compression is attained by making a high compression ratio without losing the image quality.

3.1. Discrete Tchebichef Transform (DTT)

DTT is a relatively recent transform derived from the orthonormal polynomials of Tchebichef. The size of the image block is N x N, where $tp(x)$ is the orthonormal polynomial of Tchebichef, and N is the size of the transform blocks. For block compression, this approach is acceptable as the sizes of blocks are set. However, the recursive calculation of $tp(x)$ and the

product $tp(x) tq(y)$ is mandatory, either if the block size is unknown or if the arbitrarily precise calculation of transformed coefficients is needed.

The forward Discrete Tchebichef Transform of order is characterized as:

$$T_{pq} = \sum_{x=0}^{N-1} \sum_{y=0}^{N-1} t_p(x)t_q(y)f(x,y) \tag{2}$$

$$p,q,x,y=0,\dots,N-1$$

The execution of the DTT by a simple nested loop of one multiplication over $x = 0..N-1$ and $y = 0..N-1$. The inverse transformation of DTT is defined by:

$$f(x,y) = \sum_{p=0}^{N-1} \sum_{q=0}^{N-1} T_{pq}t_p(x)t_q(y) \tag{3}$$

$$x,y, p,q=0,\dots,N-1$$

The above equation can be expressed in matrix form of series as follows

$$f(i,j) = \sum_{p=0}^{N-1} \sum_{q=0}^{N-1} T_{pq}G_{pq}(i,j) \tag{4}$$

$$p,q=0,1,\dots,N-1.$$

where G_{pq} is an 8x8 image matrix. From equation (2), where the p and q degrees can be defined inside a different 0, 1...7 domain. These can be defined over the discrete range using the following function [0, N].

$$T_p(x) = p! \sum_{k=0}^p (-1)^{p-k} \binom{p+k}{p-k} \binom{x}{p} \tag{5}$$

Due to the sizeable dynamic range of the intermediate values provided by (4), the computation of DTT values on a point-wise basis is not feasible. Rather, the function is estimated here using the following recurrence relationship:

$$t_0(x) = \frac{1}{\sqrt{N}} \tag{6}$$

$$t_1(x) = (2x+1-N) \sqrt{\frac{3}{N(N^2-1)}} \tag{7}$$

The recurrence relationship allows small numerical errors to spread by estimation, as stated by [3]. Eventually, this mistake expresses itself in the failure of

the base function [5]. The transformer block converts the initial spatial domain signal into another reduced dynamic range spatial domain signal, DTT orthogonal transform used to minimize pixel similarity, where there are only a few high energy coefficients for effective compression coefficients.

3.2. Singular Value Decomposition (SVD)

SVD is a matrix-dissecting mathematical method that breaks down a square matrix into 3 matrices of the same dimension. For example, a square matrix A of size $N \times N$ is decomposed into a matrix of U, V, and D such that matrix $A = UDV^T$ where V^T is the transpose of matrix V. U and V are orthogonal here, and D is diagonal square. That is, $UU^T = I_{rank(A)}$, $VV^T = I_{rank(A)}$, U is $rank(A) \times M$, V is $rank(A) \times N$, and D is a diagonal matrix $rank(A) \times rank(A)$.

$$D = \begin{bmatrix} \sigma_1 & 0 & \cdot & \cdot & 0 & 0 \\ 0 & \sigma_2 & \cdot & \cdot & 0 & 0 \\ \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \\ 0 & 0 & 0 & 0 & \sigma_{rank(A)-1} & 0 \\ 0 & 0 & 0 & 0 & 0 & \sigma_{rank(A)} \end{bmatrix}$$

These diagonal entries σ_i 's are called singular values of A and the number of diagonal entries is equivalent to the rank of A. These singular values satisfy the relation $\sigma_1 \geq \sigma_2 \geq \sigma_3 \dots \sigma_{rank(A)} > 0$.

3.3 Proposed DTT-SVD Compression Model

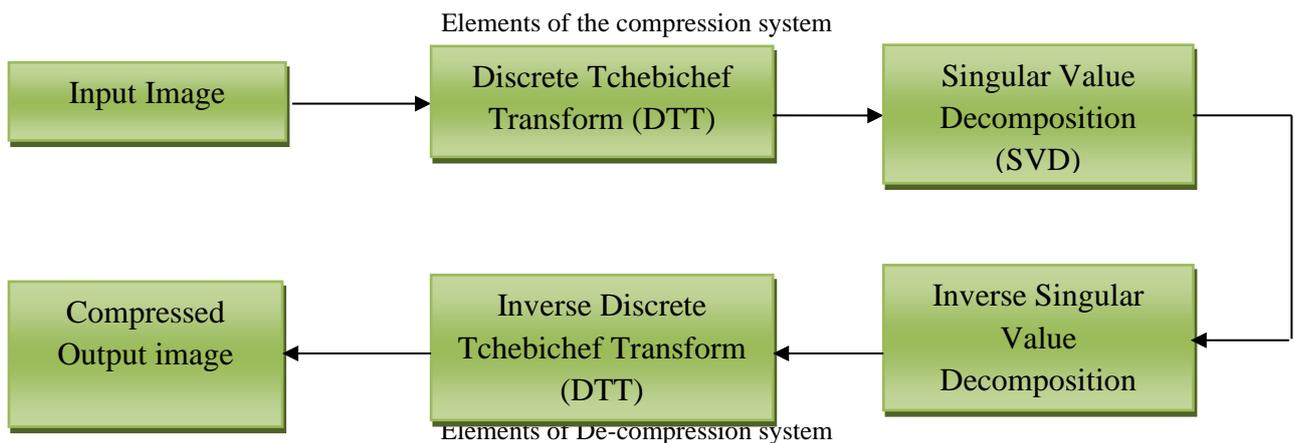


Fig1: Proposed DTT-SVD Compression Model.

The suggested approach involves several different compression methods. Initially, the Discrete Tchebichef

Each singular value defines the luminance of an image sheet, while the corresponding pair of singular vectors imply the geometry of the image [6,7]. For most of the attacks, the shift in the greatest singular value is quite small.

The columns of U are called the left singular vectors of A, and the columns of V are known as the right singular vectors of A. The Singular Value Decomposition (SVD) of A is known as this decomposition and can be composed as

$$A = UDV^T \tag{8}$$

$$SVD(A) = \sigma_1 U_1 V_1^T + \sigma_2 U_2 V_2^T + \dots + \sigma_n U_n V_n^T$$

Calculation of the SVD comprises of finding the eigenvalues, and eigenvectors of AA^T and $A^T A$. The eigenvectors of $A^T A$ frame the columns of V; the eigenvectors of AA^T frame the columns of U. In S, the singular values are the square roots of AA^T or $A^T A$ eigenvalues. The S matrix's diagonal entries are the singular values, orchestrated in descending order. Numbers that are real are always the singular values. If matrix A is a true matrix, so V and U are additionally genuine. The SVD is used to decrease the matrix's reduction in dimensionality, while the singular values σ are important while the others are small and not significant. Therefore, if the significant values are maintained and the small values are discarded, only the U and V columns corresponding to the singular values are obtained.

Transform is performed on each block of the image data in order to ensure good compression effectiveness. From

left to right and from top to bottom of the image matrix, DTT processed each block using Eq (2). High energy compaction coefficients in the DC coefficients of the matrix are derived after transformation and the remaining values are AC coefficients. Truncate the AC coefficients of the transformed matrix transformed by the DTT. For more singular value decomposition, the DC coefficients of each block value matrix will be processed to decompose into singular values. To decrease the rank of the singular matrix using Eq (8), the rank truncation procedure was used. The matrix of this image was divided into three matrices; the matrix determinant was computed using Eigenvalues and Eigenvectors. Depending on those unique values, the quality of the compression method using SVD is dependent. The important coefficients of the first components of these matrices provide a close approximation of the actual matrix, the compression performance measurement is assessed on the basis of compression ratio (CR), compression time (CT), mean square error (MSE) and peak noise ratio (PSNR). The test runs on Windows 10 and Pentium Dual-Core 2.6 GHz Processor 620 Model 3 MB Cache Processor 620 Model 3 MB Cache R2017b.

4. Performance Metrics

Lossy transformation image compression induces partial loss of bits data signal to make operation energy efficient overall for compression and lowering bits per symbol. Nevertheless, for effective image restoration, the bits of missing data need to preserve the image consistency. It is therefore necessary to verify the image compression algorithms efficiency and intensity using different performance indices.

4.1. Compression Ratio (CR)

If N_1 and N_2 represent the number of information-carrying units in the original and compressed images respectively, this is the ratio between the original image and the compressed image, so the compression ratio can be traced as CR.

$$\text{Compression Ratio (CR)} = \frac{N_1}{N_2} \quad (9)$$

4.2. Mean Square Error (MSE)

In the reconstruction, the mean squared error basically calculates the noise. Measuring the accuracy of

the average square error between the original and the compressed image is the mean square error.

$$MSE = \frac{1}{M \times N} \sum_0^{m-1} \sum_0^{n-1} ||f(i, j) - g(i, j)||^2 \quad (10)$$

4.3. Peak Signal-to-Noise Ratio (PSNR)

Taking into account the intensities in the 0-255 range, the noise power is calculated in terms of peak signal power. To achieve the accuracy of the image reconstruction, PSNR is determined. A greater PSNR suggests that the restoration of the picture is more equal to the original image.

$$\text{PSNR} = 20 \log_{10} \left(\frac{\text{MAX}_f}{\text{MSE}} \right) \quad (11)$$

4.4. Compression Time

To boost the compression speed, the compression efficiency of the execution time is determined. The time for compression and decompression is $O(n)$, where the number of pixels is n .

5. Results and Discussions

The experimental input for the proposed methods are, some sets of images with different file sizes (512*512, 256*256, 120*80) and formats such as bmp, png, tiff, jpeg, shown in Fig(1). Seven separate types of pictures, such as creatures, birds, human faces, natural, historical, and artifacts, were used to conduct the experiment. Five images are shown in their respective sections. The output is compared to the DCT-SVD algorithm using MATLAB to measure the power, accuracy, and efficiency of the proposed DTT-SVD algorithm for all kinds of possible images. Fig-3 In all cases, visual inspection of the image have been found to be good; DTT-SVD resulting from the image provides good image quality compression. Comparison is made between DCT-SVD and DTT-SVD algorithms based on the CR, PSNR, MSE, and CT parameters in Table (1), it is clear that the compression ratio of DTT-SVD is higher than that of DCT-SVD in the 0.3 to 3.3 range, it compresses the image without any quality loss, and PSNR values indicate the efficiency of the proposed approach exceeding the DCT-SVD and lesser Error (MSE), compression time over DCT-SVD.

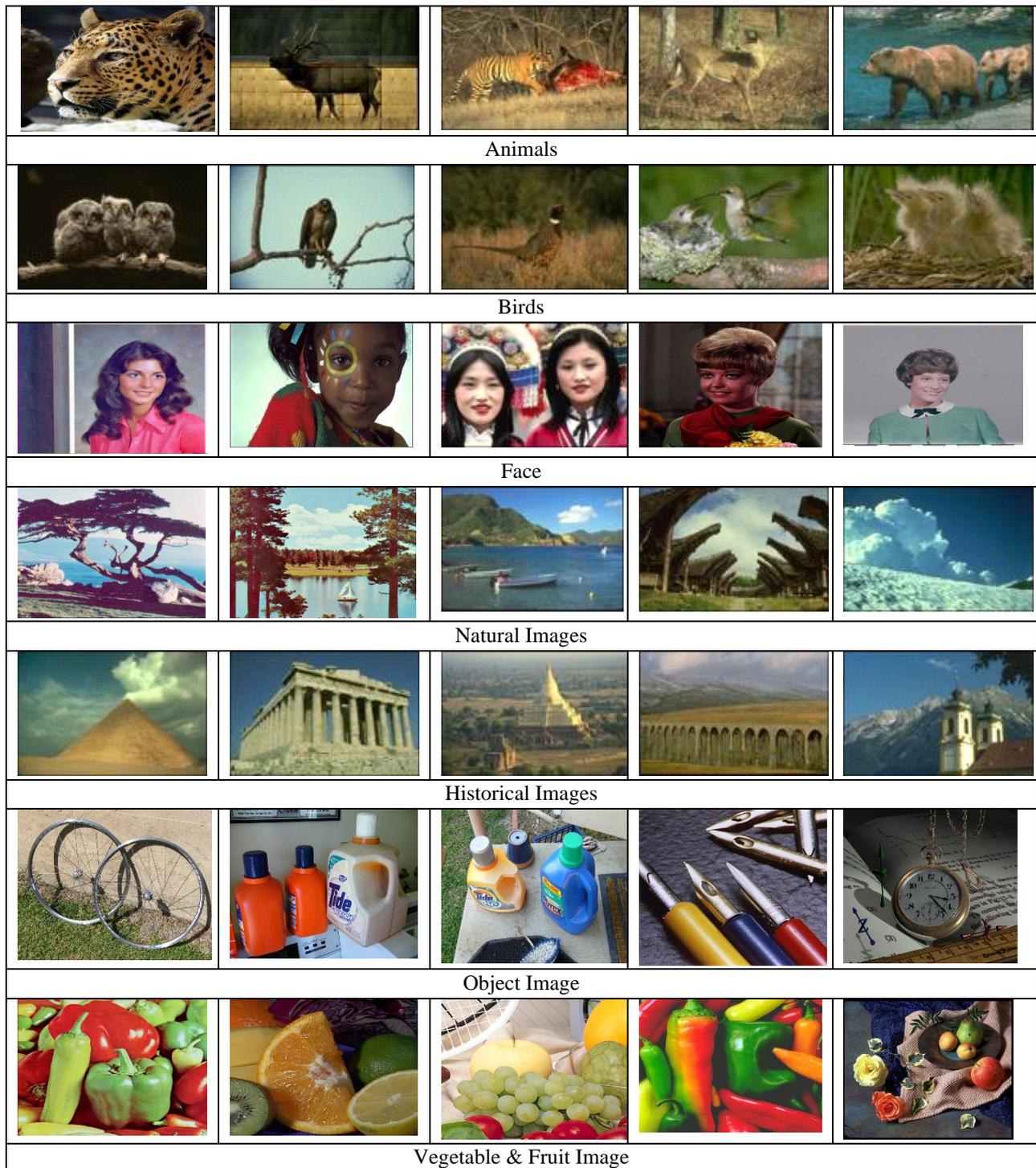


Fig-2: Category wise sample images used to experiment the compression algorithm.

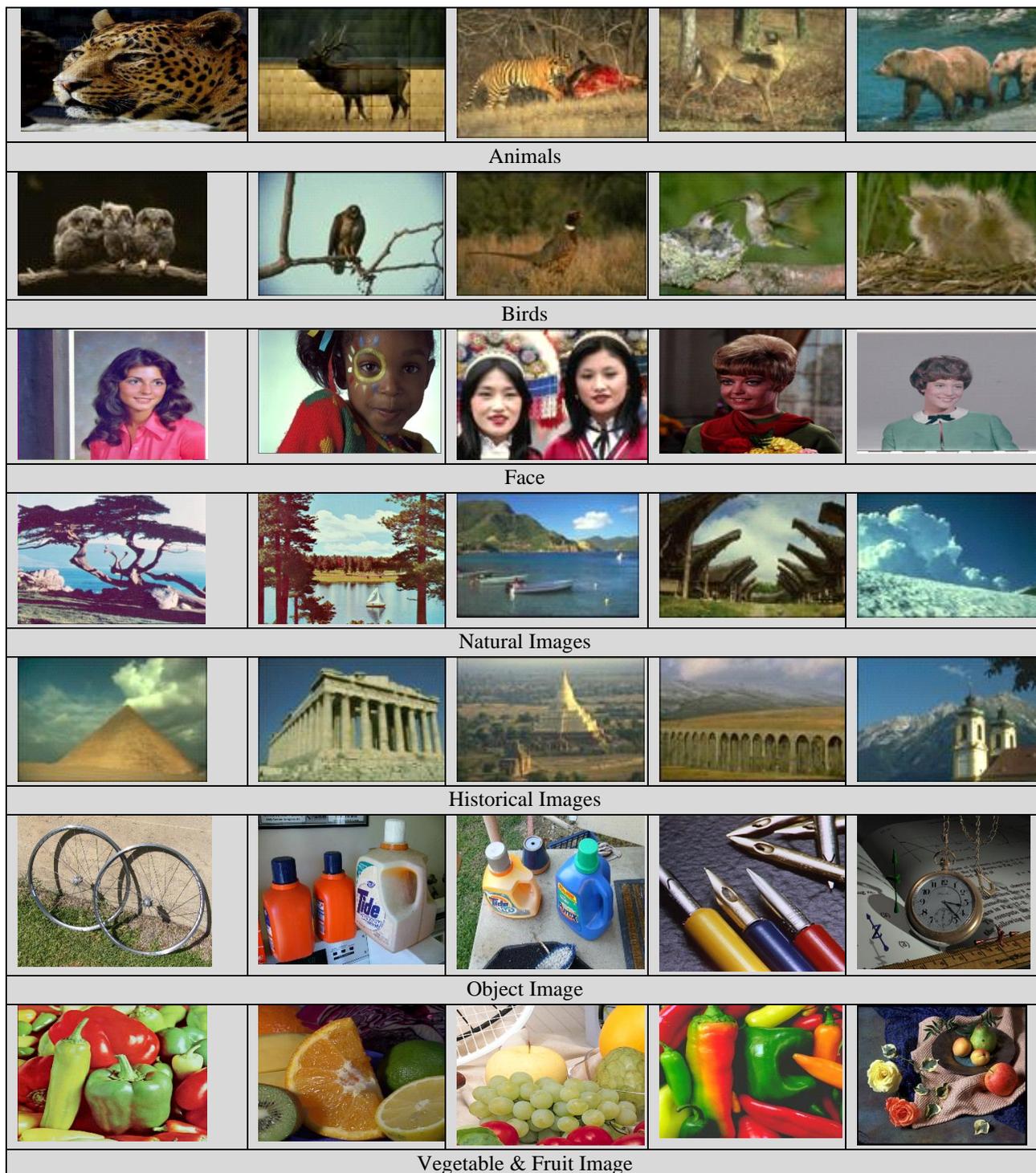


Fig-3: Category wise compressed images by using the proposed DTT-SVD algorithm.

Table 1: Experimental results of DTT-SVD and DCT-SVD

Image Group	Animals image	Birds image	Human face image	Natural image	Historical image	Object image	Vegetable image
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Performance Metrics	DTT _ SVD	DCT-SVD												
Compression Ratio(CR)	7.3	5.2	7.9	4.8	6.1	5.6	8.5	5.8	7.3	5.7	9	8.3	9.4	9.1
Mean Square Error(MSE)	83.15	82.23	80.21	80.53	82.29	82.52	100.11	107.08	68.23	68.57	90.91	90.92	101.51	101.53
PSNR(Peak signal noise ratio)	29.25	26.22	31.07	27.04	30.07	28.06	29.47	28.03	32.99	29.97	29.03	27.02	28.57	27.56
Compression Time(CT)sec	4.86	5.52	4.73	5.26	4.41	5.18	3.45	6.41	3.40	4.47	5.36	5.57	4.53	5.75

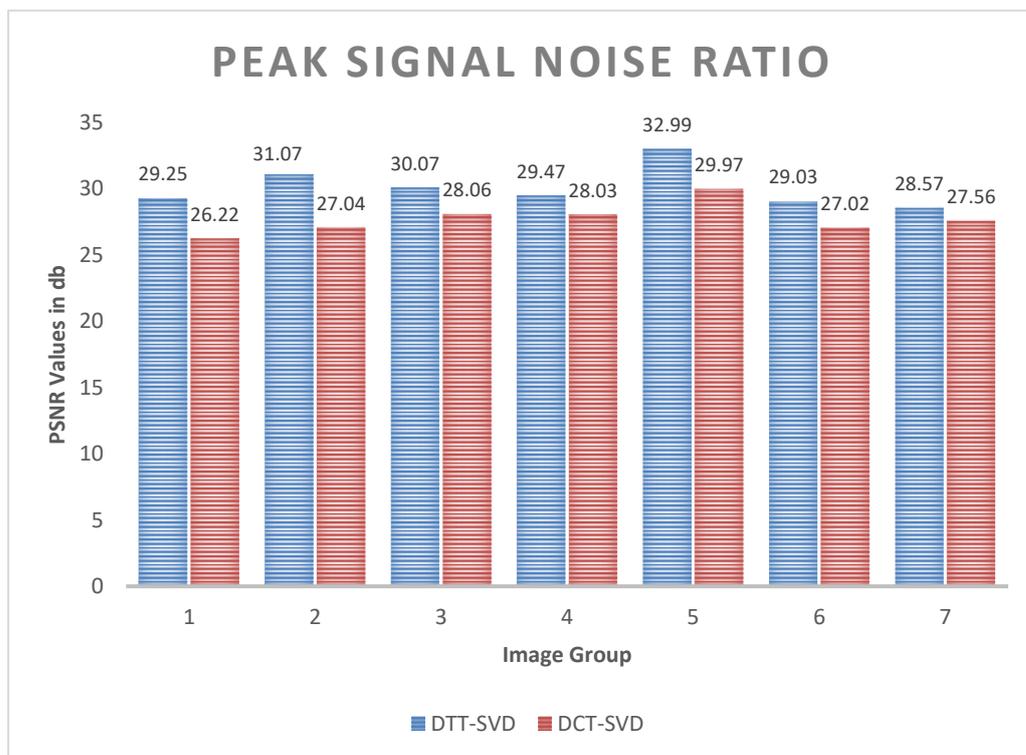


Fig.4 Comparison of DTT-SVD and DCT-SVD based on PSNR

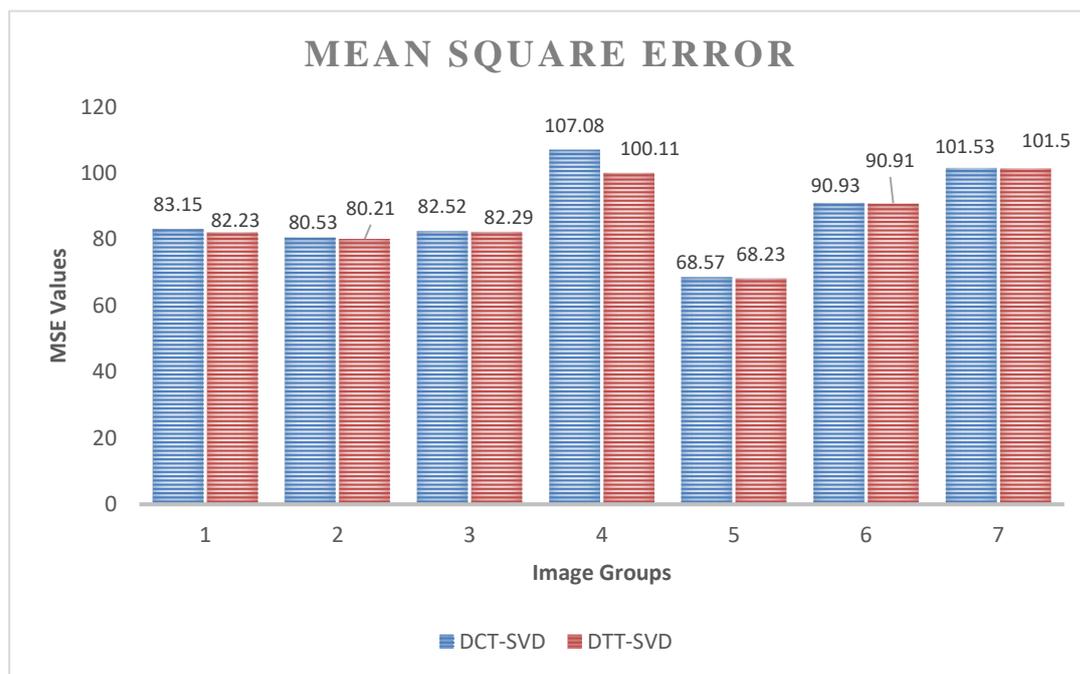


Fig.5 Comparison of DCT-SVD and DTT-SVD based on MSE

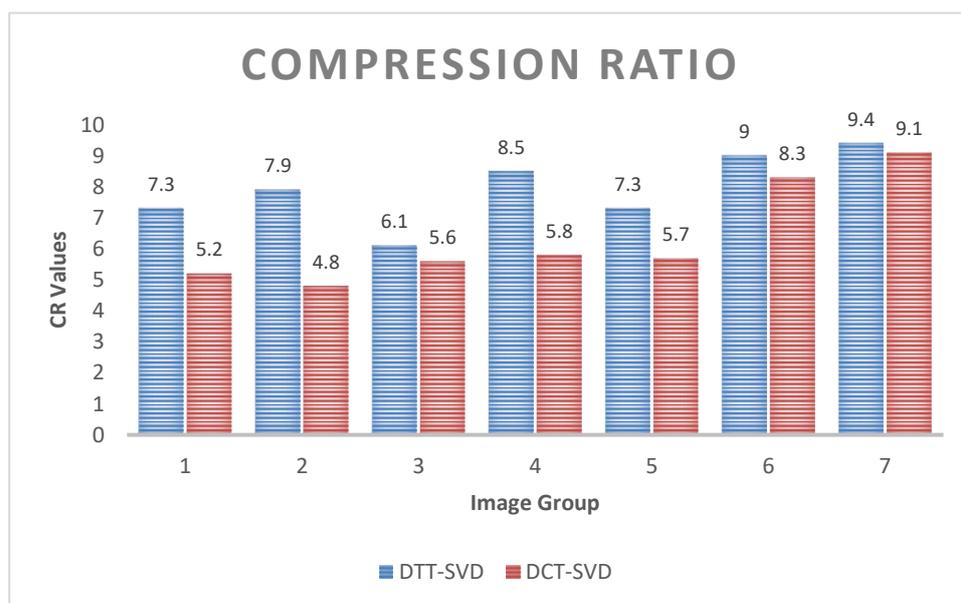


Fig.6 Comparison of DCT-SVD and DTT-SVD based on CR

From the above figure (4), it is found that the DTT-SVD PSNR tends to steadily increase from 1.01 to 4.03 in all image group sets, with a median of 1.01 differences occurring in group 7 (vegetable) as more diverse image formats have been used. Table-1 and fig (3) respectively show the experimental effects and compressed images. Figure (4) of the PSNR comparison and figure (5) of the MSE comparison show that DTT-SVD performs better than DCT-SVD. The PSNR value lies in the range of 29.97 ± 26.22 and 32.99 ± 28.57 for DCT-SVD and DTT-SVD respectively. It is obvious that all the parameters that have been obtained offer a good result and a reasonable compressed image quality. For both output metrics, the suggested approach of this study illustrates the great difference between DCT-SVD and DTT-SVD. Both case studies

indicate that the extended CR parameters are in the range of 3.3 ± 0.3 , MSE and PSNR are strongly affected after image compression and could also be due to the compression and decompression phase issue.

6. Conclusion

In this article, the results of the compression technique based on the DCT-SVD scheme show that the compression ratio and mean square error values are not satisfying. Using separate test images, the suggested DTT-SVD compression algorithm was applied. The efficiency of the proposed DTT-SVD has been found to be superior to DCT-SVD compression. Exploratory findings show that the suggested system increases the speed of compression, PSNR, and compression ratio and reduces the mean square error. A PSNR value greater than 25 is given by the proposed algorithm, which assumes the best image quality. Future research work is to develop a new algorithm which is the combination of DTT and PCA.

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