# SEGMENT RANDOM INSERTION PERTURBATION SCHEME (SRIPS) GENETIC ALGORITHM FOR MANUFACTURING INDUSTRY 

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#### Abstract

This paper lays down a formal framework for simultaneous scheduling of machines- automated guided vehicles (AGVs) and tools in a multi-machine flexible manufacturing system (FMS) while accounting for transport times of parts to minimise makespan. To minimize tooling costs- a central tool magazine (CTM) is suggested so that the tools are 'shared'. AGVs and tool transporter (TT) carry jobs and tools between machines. The complexity of including sequencing of job operations on machines- assignment of AGVs and tools to job operations and corresponding trip operations such as the empty trip and loaded trip times of AGVs and a CTM in scheduling is greater. The scope of this paper is to propose a nonlinear Mixed Integer Programming (MIP) model to minimize makespan. Since the problem is known to be NP hard- it is conjectured and then verified that the intelligent behaviour of chromosomes and genes can be effectively used to lay down a metaheuristic algorithm known as a segment random insertion perturbation scheme genetic algorithm (SRIPSGA) suitable for the problem at handand the results have been tabulated and analyzed.


Keywords: FMS- segment random insertion perturbation scheme- makespan- AGVs- Priority rules- Vehicle Scheduling- local search

## Introduction

Customer satisfaction is an important challenge in the latest manufacturing scenario- to face which- organizations have shifted their emphasis from producing large quantities of single product to a diverse mix of products with shorter life cycles. Meeting the dead lines is another crucial goal in today" s globally competitive manufacturing environment. To meet these challenges the organization should have a variety of flexibilities. In parallel with the developments in computers and automation technology over the past few decades- a new type of production system called the flexible manufacturing system (FMS) has evolved FMS is especially suitable for medium and low-volume industries. The philosophy of FMS is the right answer for unpredictable market environments that demand low-cost solutions for quickly and effectively adapting changes in product mix-demand- and designs (Viswanadham and Narahari- 1994).

One of the important aspects in FMS operation is its scheduling policy- which plays a vital role in effective utilization of resources like machines and automated material handling system.

## 2. Literature Survey

To address the complexity of the FMS scheduling problemStecke (1985) divided the FMS operation problem into preproduction setup and production operation. Set-up phase includes loading the tools- allocating the operation to the machines- allocating the pallets and fixtures to the different part types. All the issues to be handled next to setup phase are included in the production operation and he is emphasized on pre-production setup of the FMS.Kusiak (1986) presented an FMS scheduling system which uses a rule-based expert system. This system followed priority rules to schedule jobs normally- but when a job cannot be scheduled because of resource conflicts- decision tables were used to select alternative machines- tools- fixtures- material handlers. Chang et al. (1989) - report on a heuristics based beam search technique designed to solve the random FMS scheduling problem. They measured the flexibility of the manufacturing system by flexibility index and for various values of the flexibility indices they compared their algorithm against several dispatching rules. Their algorithm gave better results than the dispatching rules but at the cost of increased computational effort. Pundit and Palekar (1990) proposed branch-and-bound as well as heuristic solution procedures for the simultaneous scheduling of machines and material handling vehicles in a job-shop environment Biegel et al. (1990) applied GA to the job shop-scheduling problem and discussed the GA process for an elementary "n" tasks one-machine problem. Ulusoy et al. (1993) - pointed out to make scheduling of AGVs an integral part of the overall scheduling activity in an FMS. They proposed an iterative solution procedure to generate schedules for machines and AGVs simultaneously Chen et al. (1995) proposed a GA based heuristic for the flow shop problem on the makespan objective and compared the efficiency of the proposed GA with the other GA heuristics reported in the literature. Bilge and Ulsoy (1995) addressed the simultaneous scheduling of machines and material handling problem in an FMS environment by time window approach. They considered identical automated guided vehicles for material
transfer- which are not allowed to return to load/unload station after each delivery. Cheng et al. (1996) reviewed the research works on classical JSP using genetic algorithms. They divided their review work into two parts. In Part I- they focused their attention on the representation schemes proposed for JSP- where as in Part II- they discussed various hybrid approaches of genetic algorithms and conventional heuristics. Al-Hakim (2001) applied Genetic algorithms for solving job shop scheduling problems. He developed a new coding scheme based on grouping different levels of operations. Abdelmaguid et al. (2004) developed a hybrid GA/heuristic approach and attempted the simultaneous scheduling problem of machines and AGVs. Reddy and Rao (2006) addressed the simultaneous scheduling problem with single as well as multi-objective performance criteria including makespan- mean flow time and mean tardiness. They developed a hybrid GA- to solve the FMS scheduling problem. Jerald et al. (2006) addressed the problem of


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simultaneous scheduling of parts and AGVs for a particular type of FMS environment by using a non-traditional optimization technique called the adaptive genetic algorithm (AGA). Gonçalves et al. (2002) have developed a hybrid genetic algorithm for the job shop scheduling problem. The chromosome representation of the problem was based on random keys. Aytug et al. (2003) thoroughly reviewed the literature on application of genetic algorithms for production and operations management problems. Nearchou (2004) investigated the effect of various genetic operators on the performance of GAs when applied on permutation flow-shop scheduling problems..

## 3. Scheduling Problem

Simultaneous scheduling problems in FMS with four layout configurations as shown in Fig. 1 and ten job sets are used (Bilge and Ulsoy, 1995). The AGV travel times and the machine allocation and operation times for the jobs are given in Appendix A
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Figure: 1 Layout configurations used for examples

## 4. Simultaneous Scheduling of machines and AGVs in FMS

Jobs are scheduled based on the operation sequence derived by the algorithms. The problem considered needs scheduling of material handling system along with that of machines. In this paper SRIPSGA are used to solve simultaneous scheduling problems which are discussed below

The steps involved in SRIPSGA are given below:
Step 1: Genetic representation
Step 2: Initial Population
Step 3: Evaluation Function

Step 4: Reproduction selection Scheme
Step 5: Genetic Operators
Step 6: Incorporate a local search in to the GA
Step 7: Receptor Editing
Step 8: Termination criterion
Step 9: Genetic Algorithm parametric setting

### 4.1 Simultaneous Scheduling through SRIPSGA

For implementation of SRIPSGA- Job set 5 and Layout 2 are considered as an example. SRIPSGA computes the process times for different jobs and the sequences are obtained based
on the random manner.
The SRIPSGA is explained in the following steps for the job set 5 :

### 4.1.1 Genetic Representation

Proper representation plays a vital role in successful implementation of any evolutionary algorithm. Here
operations based coding (Gen and Cheng- 1997) is used to represent genes in a particular chromosome- where every gene is represented by a number. Hence the chromosome consists of as many numbers of genes as the total number of operations in that job set.

| Job <br> Number | 1 |  |  | 2 |  |  | 3 |  |  | 4 |  | 5 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Operation number | 1 | 2 | 3 | 1 | 2 | 3 | 1 | 2 | 3 | 1 | 2 | 1 | 2 |
| Gene Code | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 |
| Machine number | M1 | M2 | M4 | M1 | M3 | M2 | M3 | M4 | M1 | M4 | M2 | M3 | M1 |
| Processing time | 8 | 16 | 12 | 20 | 10 | 18 | 12 | 8 | 15 | 14 | 18 | 10 | 15 |

### 4.1.2 Initial Population

Double the number of operations is used in this paper- i.e. a list of jobs is itself taken as an operations. For example- if in a flow shop scenario there are 5 jobs with 13 operations it

| Chromosome number | Chromosome |
| :---: | :---: |
| 1 | 4-10-12-1-7-2-13-5-11-8-3-6-9 |
| 2 | 4-10-12-1-7-2-8-13-11-5-9-6-3 |
| 3 | 10-12-1-7-4-13-11-2-8-5-9-6-3 |
| 4 | 4-10-12-7-1-11-13-2-8-5-6-3-9 |
| 5 | 4-12-1-7-10-2-5-11-13-8-9-6-3 |
| 6 | 1-10-7-4-12-8-2-11-13-5-3-6-9 |
| 7 | 7-12-1-4-10-13-2-8-11-5-6-9-3 |
| 8 | 7-10-12-4-1-13-2-5-11-8-3-9-6 |
| 9 | 1-4-10-12-7-8-13-2-5-11-3-9-6 |
| 10 | 12-10-1-7-4-8-13-2-5-11-9-6-3 |
| 11 | 10-7-12-4-1-11-8-13-5-2-9-3-6 |
| 12 | 1-4-12-10-7-2-13-11-8-5-6-3-9 |
| 13 | 7-4-10-12-1-5-11-2-13-8-6-3-9 |
| 14 | 7-10-1-4-12-8-5-11-13-2-3-6-9 |
| 15 | 4-1-7-12-10-5-13-2-11-8-6-3-9 |
| 16 | 7-1-10-12-4-11-13-8-5-2-6-9-3 |


| 17 | 4-12-7-10-1-8-13-11-2-5-6-3-9 |
| :---: | :---: |
| 18 | 12-4-10-7-1-11-5-8-13-2-9-3-6 |
| 19 | 12-7-10-1-4-2-5-8-13-11-9-3-6 |
| 20 | 7-12-10-4-1-8-11-2-13-5-3-6-9 |
| 21 | 12-1-7-10-4-5-2-13-8-11-9-3-6 |
| 22 | 10-4-12-7-1-2-8-5-13-11-9-3-6 |
| 23 | 12-10-4-7-1-2-11-13-8-5-9-3-6 |
| 24 | 7-4-12-1-10-5-8-13-11-2-3-6-9 |
| 25 | 1-4-10-12-7-13-11-8-2-5-3-6-9 |
| 26 | 4-7-1-12-10-13-11-8-2-5-3-9-6 |

### 4.1.3 Evaluation Function

For implementation of SRIPSGA Algorithm- job set 5 and layout 2 are considered as an example. From the above population job order operation sequence ' 1 ' is
4-10-12-1-7-2-13-5-11-8-3-6-9
For identifying the maximum operational completion time of the above sequence- the steps discussed in below are executed.
Step 1: Considering the machine number (M.No) of the given sequence for the job
M1-M4-M3-M1-M3- M2-M1-M3-M2-M4-M4-M2-M1
Step 2: The AGV ' 1 ' is selected
Step 3: The vehicle's previous location (VPL) is identified
For example considering first operation VPL=L/U
Step 4: The previous operation machine number (POMN) is identified as

## POMN=L/U

Step 5: The vehicle ready time (VRT) is identified as VRT=0
Step 6: The previous operation completion time (POCT) is found to be ' 0 '
Step 7: Vehicle empty trip time (VET) is calculated with $\mathrm{VET}=\mathrm{VRT}+\mathrm{TRT} 1=0+0=0$ Where TRT1 = VPL to $\mathrm{POMN}=\mathrm{L} / \mathrm{U}$ to $\mathrm{L} / \mathrm{U}=0$
Step 8: The maximum vehicle empty travel time is found from
$\operatorname{Max}(\mathrm{VET})=$ Maximum $($ POCT and VET $)=\operatorname{Max}(0-$
$0)=0$
Step 9: The total travel time of vehicle (TT) is evaluated from

TT=VET+ Time taken from previous machine to latest machine.

| O.No | M.No | V.No | VPL | POMN | VRT | POCT | VET | $\operatorname{Max}(7,8)$ | VLT | MRT | $\operatorname{Max}(10,11)$ | Process <br> Time | Make <br> Span |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |


| $(1)$ | $(2)$ | $(3)$ | $(4)$ | $(5)$ | $(6)$ | $(7)$ | $(8)$ | $(9)$ | $(10)$ | $(11)$ | $(12)$ | $(13)$ | $(14)$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 4 | M1 | 1 | $\mathrm{~L} / \mathrm{U}$ | $\mathrm{L} / \mathrm{U}$ | 0 | 0 | 0 | 0 | 2 | 0 | 2 | 18 | 38 |
| 10 | M 4 | 2 | $\mathrm{~L} / \mathrm{U}$ | $\mathrm{L} / \mathrm{U}$ | 0 | 0 | 0 | 0 | 3 | 0 | 3 | 6 | 15 |
| 12 | M 3 | 2 | 4 | $\mathrm{~L} / \mathrm{U}$ | 3 | 0 | 5 | 5 | 9 | 0 | 9 | 3 | 15 |
| 1 | M 1 | 1 | 1 | $\mathrm{~L} / \mathrm{U}$ | 2 | 0 | 5 | 5 | 7 | 38 | 38 | 6 | 50 |
| 7 | M 3 | 1 | 1 | $\mathrm{~L} / \mathrm{U}$ | 7 | 0 | 10 | 10 | 14 | 15 | 15 | 9 | 33 |
| 2 | M 2 | 2 | 3 | 1 | 9 | 50 | 14 | 50 | 51 | 0 | 51 | 12 | 75 |
| 13 | M 1 | 1 | 3 | 3 | 14 | 15 | 14 | 15 | 20 | 50 | 50 | 9 | 68 |
| 5 | M 3 | 1 | 1 | 1 | 20 | 38 | 20 | 38 | 40 | 33 | 40 | 6 | 52 |
| 11 | M 2 | 1 | 3 | 4 | 40 | 15 | 41 | 41 | 46 | 75 | 75 | 15 | 105 |
| 8 | M 4 | 1 | 2 | 3 | 46 | 33 | 47 | 47 | 48 | 15 | 48 | 3 | 54 |
| 3 | M4 | 2 | 2 | 2 | 51 | 75 | 51 | 75 | 77 | 54 | 77 | 9 | 95 |
| 6 | M2 | 1 | 4 | 3 | 48 | 52 | 54 | 54 | 60 | 105 | 105 | 15 | 135 |
| 9 | M1 | 1 | 2 | 4 | 60 | 54 | 62 | 62 | 66 | 68 | 68 | 12 | 92 |

Table 1 shows operation scheduling of through SRIPSGA rule for job set 5 layout 2 is shown. From the vehicle heuristic algorithm for first two operations AGVs are selected sequentially in case of third operation AGV ' 2 ' is selected basing on the availability of AGV with minimum travel time this constraint will be taking care in the algorithm. For job set 5 and layout 2 the operational completion time (makespan) is 135
In similar way make span for all 26 sequences are calculate and identify the best sequences based on evaluation function for the reproduction selection scheme

### 4.1.4 Reproduction Selection Scheme

Receptor Editing Genetic Algorithm uses tournament selection procedure is used in this work- which picks randomly "Chromosomes and the winner (based on their fitness) among them is selected for next operation.

### 4.1.5 Genetic Operators

In order to alter the genetic alignment and to reproduce new chromosomes in every generation genetic operation like crossover and mutation are performed.

### 4.1.6 Crossover operators

The crossover operator is an important component of GA. The crossover operation generates offspring from randomly selected pairs of individuals within the mating pool- by exchanging segments of the chromosome strings from the parents. Different types of crossover operators are available in the literature and here in this work- single point crossover and two-point crossover are considered.
i) Single point crossover:

In single point crossover randomly a cut point is selected and one side of the genes of the cut point in the first parent is exchanged with the genes of second parent on the same side.
Chromosomes before single point crossover:

## 4-10-12-1-7-|2-13-5-11-8-3-6-9

## 10-12-1-7-4-13-11-2-8-5-9-6-3

Chromosomes after single point crossover:
4-10-12-1-7-2-111-2-8-5-9-6-3
10-12-1-7-4-13-13-5-11-8-3-6-9
As it can be seen the off springs produced after crossover may violate the precedence constraints and also some genes may be missing whereas others are duplicated. In the present case operations 2 is duplicated whereas operations 13 is missing in offspring 1 . The reverse is true in offspring 2 i.e.13 duplicated and 2 is missing. To take care of these problems repair and replace functions are used. Repair function exchanges the genes to yield valid off-springs whereas replace function removes the duplicate genes and replaces them with missing genes.
Chromosomes after single point crossover replace and repair:
4-10-12-1-7-2-11-13-8-5-9-6-3
10-12-1-7-4-13-13-5-11-8-3-6-9

## ii) Two-point crossover:

As the name indicates- in this case two cut points are selected randomly and the genes in between these cut points are exchanged.

Chromosomes before two-point crossover:
4-10-12-1ł7-2-11-13-8-5-9-6-3
10-12-1-7 4-13-13-5-11-8-3-6-9
Similar to single point crossover here also the problems like violation of precedence constraints- duplication and missing of genes may arise which needs repair and replace.
Chromosomes after two-point crossover- replace and repair
4-10-12-1-7-2-13-8-11-5-9-6-3
10-12-1-7-4-2-11-13-8-5-3-6-9

### 4.1.7 Mutation operators

For exploring the search space effectively- now mutation operation is performed on the selected chromosomes. Different mutation operators are available in the literature and among them random mutation- inverse mutationadjacent mutation and shift mutation are used in this work and the performance of the GA for different mutations in combination with the above two crossover operators is studied.

## Random Mutation

In this mutation two genes are randomly selected and their positions are exchanged. If necessary- chromosome is repaired.
Chromosome before random mutation:
10-12-1-7-4-2-11-13-8-5-3-6-9
Chromosome after random mutation:
10-12-1-7-13-2-11-4-8-5-3-6-9

## Adjacent Mutation

In this case two genes which are adjacent to each other are exchanged.
Chromosome before adjacent mutation:
10-12-1-7-13-2-11-4-8-5-3-6-9
Chromosome after adjacent mutation:
10-12-1-7-2-13-11-4-8-5-3-6-9

## Inverse Mutation:

Here a set of successive genes are selected and the entire set is reversed and if this leads to infeasible chromosome then it is repaired.
Chromosome before inverse mutation:
10-12-1-7-2-13-11-4-8-5-3-6-9

Chromosome after inverse mutation and before \& after repair

10-12-1-4-11-13-2-7-8-5-3-6-9

## Shift Mutation

In this mutation a gene is selected randomly- and it is shifted to another randomly selected position and again if necessaryit is repaired.
Chromosome before shift mutation:
10-12-1-4-11-13-2-7-8-5-3-6-9
Chromosome after shift mutation:
10-12-1-4-11-5-13-2-7-8-3-6-9

Similar to crossover- here also there is a possibility of violation of precedence constraints after mutation operation which is taken care of again by the repair function.

### 4.1.8 Incorporate a local search into the GA

In this work a local search called Segment Random Insertion Perturbation Scheme (SRIPS) is used. According to this local search for each sequence obtained after mutation, few more neighbors are created and the best among them will be transferred in to the next generation. The following steps explain the local search procedure.
Step 1: Consider the chromosome which is generated after crossover and mutation.
10-12-1-4-11-5-13-2-7-8-3-6-9
Step 2: Select randomly a sub-segment (S), of size "p".
$\mathrm{S}=11-5-13-2-7$ and $\mathrm{P}=5$
Step 3: Insert any one member of the sub-segment at one of the randomly selected position, to the left or right of the subsegment.
10-12-11-1-4--5-13-2-7-8-3-6-9
Insertion to left creates a neighbor to the sequence and Insertion to right creates another neighbor to the sequence.
10-12-1-4-5-13-11-2-7-8-3-6-9
Step 4: Repeat step 3, till all the members in the subsequence are selected. This creates " 2 p " neighbors.
Step 5: Compute the fitness of all the neighbors created and sort them in the descending order of their fitness. Select the fittest members among the neighbors

### 4.1.9 Receptor Editing Scheme for creating new generation:

The editing of the chromosomes in the population after the cross over operation is known as receptor editing. In this process a number of worst makespan value chromosomes are eliminated from the population and randomly generated chromosomes are added in those places. After editing the chromosomes in the population- the new population has gone to next iteration until termination criterion is reached. This concept is adopted from

### 4.1.10 Termination

The process of selection- crossover and mutation are repeated till the termination criterion is satisfied. In this work the number of generations is taken as the termination criterion- which is varied from 100 to 1000 generations and its effect on the performance of the algorithm is noted down.

### 4.1.11 Genetic Algorithm parametric setting

Genetic algorithm's evolutionary procedure has been implemented in JAVA language and simulated for various problem sets. Population size is taken as twice the chromosome length (total number of operations in the job set). The results are obtained after repeating the evolutionary procedure for 20 runs and the number of generations is varied from 100 to 1000 . Crossover rate $20 \%, 30 \%, 40 \%$ and $50 \%$, Mutation rate is $0.02 \%, 0.04 \%, 0.06 \%$ \& $0.08 \%$,

## Receptor Editing 10\% and 20\%

## 5. Computational Analysis

The proposed method has now been applied to the benchmark problems given by Bilge and Ulusoy (1995) with extra data on the tools needed to perform the operation. These benchmark problems were generated at different levels of travel times to processing times ( $\mathrm{t} / \mathrm{p}$ ) ratio. These benchmark problems were produced with the proportion of
processing times ( $\mathrm{t} / \mathrm{p}$ ) at distinct rates of travel times. Ten job sets, 4 layouts and 2 AGVs were combined to design the 120 test problems, 40 with $\mathrm{t} / \mathrm{p}>0.25$ and 80 with $\mathrm{t} / \mathrm{p}<0.25$. Three cases with 4 distinct layouts (LY1, LY2, LY3 and LY4) were considered here for makespan calculation with growing processing times. Original processing times were employed in Table 2 where the processing times were doubled and tripled respectively, as in Table 3 and Table 4.

Table 2: Performance analysis ( $\mathrm{t} / \mathrm{p}>0.25$ )

| Job. No | t/p | FCFS | SPT | LPT | SRIPSGA |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1.1 | 0.59 | 173 | 193 | 177 | 94 |
| 2.1 | 0.61 | 158 | 158 | 177 | 104 |
| 3.1 | 0.59 | 202 | 224 | 198 | 112 |
| 4.1 | 0.91 | 263 | 267 | 264 | 113 |
| 5.1 | 0.85 | 148 | 164 | 148 | 84 |
| 6.1 | 0.78 | 231 | 240 | 227 | 124 |
| 7.1 | 0.78 | 195 | 210 | 201 | 120 |
| 8.1 | 0.58 | 261 | 261 | 266 | 185 |
| 9.1 | 0.61 | 270 | 277 | 268 | 120 |
| 10.1 | 0.55 | 308 | 308 | 310 | 174 |
| 1.2 | 0.47 | 143 | 173 | 165 | 76 |
| 2.2 | 0.49 | 124 | 124 | 130 | 77 |
| 3.2 | 0.47 | 162 | 188 | 160 | 87 |
| 4.2 | 0.73 | 217 | 223 | 224 | 85 |
| 5.2 | 0.68 | 118 | 144 | 131 | 73 |
| 6.2 | 0.54 | 180 | 169 | 165 | 104 |
| 7.2 | 0.62 | 149 | 160 | 149 | 85 |
| 8.2 | 0.46 | 181 | 181 | 198 | 159 |
| 9.2 | 0.49 | 250 | 249 | 244 | 105 |
| 10.2 | 0.44 | 290 | 288 | 287 | 152 |
| 1.3 | 0.52 | 145 | 175 | 167 | 82 |
| 2.3 | 0.54 | 130 | 130 | 136 | 82 |
| 3.3 | 0.51 | 160 | 190 | 162 | 89 |


| 4.3 | 0.8 | 233 | 237 | 230 | 94 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 5.3 | 0.74 | 120 | 146 | 133 | 70 |
| 6.3 | 0.54 | 182 | 171 | 167 | 112 |
| 7.3 | 0.68 | 155 | 166 | 151 | 87 |
| 8.3 | 0.5 | 183 | 183 | 200 | 169 |
| 9.3 | 0.53 | 252 | 251 | 246 | 108 |
| 10.3 | 0.49 | 293 | 294 | 293 | 158 |
| 1.4 | 0.74 | 189 | 207 | 189 | 104 |
| 2.4 | 0.77 | 174 | 174 | 174 | 107 |
| 3.4 | 0.74 | 220 | 250 | 212 | 126 |
| 4.4 | 1.14 | 301 | 301 | 298 | 128 |
| 5.4 | 1.06 | 171 | 189 | 171 | 97 |
| 6.4 | 0.78 | 249 | 252 | 237 | 133 |
| 7.4 | 0.97 | 217 | 242 | 151 | 135 |
| 8.4 | 0.72 | 285 | 285 | 200 | 195 |
| 9.4 | 0.76 | 292 | 311 | 290 | 125 |
| 10.4 | 0.69 | 350 | 350 | 345 | 182 |

In the optimal sequence of machines and AGVs are determined by using FCFS- SPT- LPT and SRIPSGA for T/P>0.25 and shown in Table no 2. From table 2- out of 40 Table 3: Performance analysis ( $\mathrm{t} / \mathrm{p}<0.25$ )

| Job.No | t/p | FCFS | SPT | LPT | SRIPSGA |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1.10 | 0.15 | 207 | 248 | 252 | 121 |
| 2.10 | 0.15 | 217 | 217 | 225 | 130 |
| 3.10 | 0.15 | 257 | 327 | 282 | 162 |
| 4.10 | 0.15 | 303 | 328 | 317 | 119 |
| 5.10 | 0.21 | 152 | 190 | 187 | 93 |
| 6.10 | 0.16 | 304 | 281 | 297 | 194 |
| 7.10 | 0.19 | 231 | 240 | 264 | 137 |
| 8.10 | 0.14 | 338 | 338 | 347 | 292 |
| 9.10 | 0.15 | 390 | 367 | 359 | 185 |


| 10.10 | 0.14 | 452 | 429 | 444 | 267 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1.20 | 0.12 | 194 | 238 | 246 | 122 |
| 2.20 | 0.12 | 194 | 194 | 206 | 130 |
| 3.20 | 0.12 | 241 | 311 | 270 | 159 |
| 4.20 | 0.12 | 285 | 312 | 298 | 116 |
| 5.20 | 0.17 | 142 | 180 | 184 | 92 |
| 6.20 | 0.12 | 292 | 260 | 284 | 174 |
| 7.20 | 0.15 | 212 | 218 | 249 | 136 |
| 8.20 | 0.11 | 306 | 319 | 334 | 287 |
| 9.20 | 0.12 | 380 | 355 | 347 | 179 |
| 10.20 | 0.11 | 445 | 423 | 439 | 260 |
| 1.30 | 0.13 | 195 | 239 | 247 | 117 |
| 2.30 | 0.13 | 197 | 197 | 209 | 126 |
| 3.30 | 0.13 | 240 | 312 | 271 | 160 |
| 4.30 | 0.13 | 292 | 317 | 301 | 117 |
| 5.30 | 0.18 | 141 | 181 | 183 | 91 |
| 6.30 | 0.24 | 296 | 261 | 285 | 192 |
| 7.30 | 0.17 | 215 | 221 | 250 | 137 |
| 8.30 | 0.13 | 307 | 320 | 335 | 288 |
| 9.30 | 0.13 | 381 | 356 | 348 | 180 |
| 10.30 | 0.12 | 448 | 426 | 442 | 270 |
| 1.40 | 0.18 | 213 | 255 | 254 | 120 |
| 2.40 | 0.13 | 221 | 221 | 228 | 136 |
| 3.40 | 0.18 | 261 | 330 | 282 | 162 |
| 4.40 | 0.19 | 315 | 336 | 323 | 120 |
| 5.40 | 0.18 | 155 | 197 | 186 | 98 |
| 6.40 | 0.19 | 310 | 288 | 299 | 180 |
| 7.40 | 0.24 | 239 | 251 | 270 | 137 |
| 8.40 | 0.18 | 343 | 343 | 349 | 293 |


| 9.40 | 0.19 | 396 | 379 | 370 | 182 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 10.40 | 0.17 | 466 | 445 | 455 | 266 |

In the optimal sequence of machines and AGVs are determined by using FCFS- SPT- LPT and SRIPSGA for T/P $<0.25$ and shown in Table no 3. From Table 3 - out of 40
Table 4: Performance analysis ( $\mathrm{t} / \mathrm{p}<0.25$ )

| Job.No | t/p | FCFS | SPT | LPT | SRIPSGA |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1.11 | 0.15 | 290 | 349 | 361 | 177 |
| 2.11 | 0.15 | 299 | 299 | 316 | 196 |
| 3.11 | 0.15 | 366 | 473 | 411 | 239 |
| 4.11 | 0.15 | 426 | 467 | 448 | 175 |
| 5.11 | 0.21 | 215 | 262 | 271 | 138 |
| 6.11 | 0.16 | 443 | 398 | 433 | 286 |
| 7.11 | 0.19 | 325 | 334 | 379 | 203 |
| 8.11 | 0.14 | 488 | 488 | 508 | 433 |
| 9.11 | 0.15 | 560 | 521 | 509 | 269 |
| 10.11 | 0.14 | 652 | 617 | 641 | 395 |
| 1.21 | 0.12 | 280 | 339 | 358 | 178 |
| 2.21 | 0.12 | 276 | 276 | 297 | 183 |
| 3.21 | 0.12 | 350 | 457 | 399 | 236 |
| 4.21 | 0.12 | 407 | 450 | 429 | 172 |
| 5.21 | 0.17 | 205 | 252 | 268 | 137 |
| 6.21 | 0.12 | 432 | 377 | 420 | 290 |
| 7.21 | 0.15 | 299 | 315 | 364 | 202 |
| 8.21 | 0.11 | 469 | 469 | 495 | 428 |
| 9.21 | 0.12 | 550 | 509 | 497 | 266 |
| 10.21 | 0.11 | 645 | 612 | 638 | 386 |
| 1.31 | 0.13 | 279 | 340 | 357 | 175 |
| 2.31 | 0.13 | 279 | 279 | 300 | 192 |
| 3.31 | 0.13 | 349 | 458 | 400 | 237 |
| 4.31 | 0.13 | 412 | 453 | 430 | 173 |


| 5.31 | 0.18 | 204 | 253 | 267 | 136 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 6.31 | 0.24 | 433 | 378 | 421 | 276 |
| 7.31 | 0.17 | 302 | 318 | 365 | 203 |
| 8.31 | 0.13 | 470 | 470 | 496 | 429 |
| 9.31 | 0.13 | 551 | 510 | 498 | 267 |
| 10.31 | 0.12 | 648 | 615 | 641 | 387 |
| 1.41 | 0.18 | 296 | 356 | 363 | 176 |
| 2.41 | 0.13 | 307 | 307 | 319 | 193 |
| 3.41 | 0.18 | 370 | 476 | 411 | 239 |
| 4.41 | 0.19 | 434 | 471 | 451 | 176 |
| 5.41 | 0.18 | 218 | 269 | 270 | 137 |
| 6.41 | 0.19 | 445 | 405 | 433 | 281 |
| 7.41 | 0.24 | 329 | 344 | 385 | 203 |
| 8.41 | 0.18 | 493 | 493 | 508 | 434 |
| 9.41 | 0.19 | 560 | 533 | 520 | 269 |
| 10.41 | 0.17 | 666 | 633 | 652 | 391 |

In the optimal sequence of machines and AGVs are determined by using FCFS- SPT- LPT and SRIPSGA for T/P<0.25 and shown in Table no 4. From Table 4 out of 40 problems 40 problems gives improved results using SRIPSGA in comparison with FCFS- SPT and LPT

## 6. Conclusions

The purpose of this research work is to provide an integrated schedule for minimum makespan and also to study the impact of considering machines, AGVs and job transfer times in a multi machine FMS for simultaneous scheduling.FMS scheduling plays an effective and vital role in efficient utilization of resources. This problem being an NP hard, a metaheuristic optimisation algorithm, called SRIPSGA is developed for solving this optimization problem. This scheduling problem is about integrating the assignment of the appropriate machine-AGV-tool combination into each job operation and sequencing and timing of those job operations while constraints are imposed on the system. The results show that tool waiting time and job transfer time between machines have significant influence on makespan. Hence, it is confirmed that by omitting the tool waiting and job transfer times will make the result of scheduling non-realistic. The program developed can be adapted to any layout configuration provided change
in AGV travel time matrix in input data. The work can be explored further by considering the transfer times of tools between machines and tool shift activities caused by tool wear.

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| Layout-1 |  |  |  |  |  |  | L/U | M1 | M2 | M3 | M4 |
| :--- | :--- | :--- | :--- | :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| From/To | 0 | 6 | 8 | 10 | 12 |  |  |  |  |  |  |
| L/U | 12 | 0 | 6 | 8 | 10 |  |  |  |  |  |  |
| M1 | 10 | 6 | 0 | 6 | 8 |  |  |  |  |  |  |
| M2 | 8 | 8 | 6 | 0 | 6 |  |  |  |  |  |  |
| M3 | 6 | 10 | 8 | 6 | 0 |  |  |  |  |  |  |
| M4 |  |  |  |  |  |  |  |  |  |  |  |


| Layout-3 |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :---: |
| From/To | L/U | M1 | M2 | M3 | M4 |  |

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## APPENDIX A

Travel time matrix for this particular problem

| Layout-2 |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| From/To | L/U | M1 | M2 | M3 | M4 |
| L/U | 0 | 4 | 6 | 8 | 6 |
| M1 | 6 | 0 | 2 | 4 | 2 |
| M2 | 8 | 12 | 0 | 2 | 4 |
| M3 | 6 | 10 | 12 | 0 | 2 |
| M4 | 4 | 8 | 10 | 12 | 0 |


| Layout-4 |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :---: |
| From/To | L/U | M1 | M2 | M3 | M4 |  |


| L/U | 0 | 2 | 4 | 10 | 12 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| M1 | 12 | 0 | 2 | 8 | 10 |
| M2 | 10 | 12 | 0 | 6 | 8 |
| M3 | 4 | 6 | 8 | 0 | 2 |
| M4 | 2 | 4 | 6 | 12 | 0 |


| L/U | 0 | 4 | 8 | 10 | 14 |
| :--- | :--- | :--- | :--- | :--- | :---: |
| M1 | 18 | 0 | 4 | 6 | 10 |
| M2 | 20 | 14 | 0 | 8 | 6 |
| M3 | 12 | 8 | 6 | 0 | 6 |
| M4 | 14 | 14 | 12 | 6 | 0 |

Data for the Job Sets Used in Example Problems

| JobSet-1 | JobSet-2 |
| :---: | :---: |
| Job 1: M1(8); M2(16); M4(12) | Job 1: Ml(10); M4(18) |
| Job 2: Ml(20); M3(10); M2(18) | Job 2: M2(10); M4(18) |
| Job 3: M3(12); M4(8); Ml(15) | Job 3: Ml(10); M3(20); |
| Job 4: M4(14); M2(18) | Job 4: M2(10); M3(15); M4(12) |
| Job 5: M3(10); Ml(15) | Job 5: Ml(10); M2(15); M4(12) |
|  | Job 6: M1(10); M2(15); M3(12) |
| JobSet-3 | JobSet-4 |
| Job 1:M1(16); M3(15) | Job1: M4(11); M1(10); M2(7) |
| Job 2:M2(18); M4(15) | Job2: M3(12); M2(10); M4(8) |
| Job 3: Ml(20); M2(10) | Job3: M2(7); M3(10); M1(9); M3(8) |
| Job 4:M3(15); M4(10) | Job4: M2(7); M4(8); M1(12);M2(6) |
| Job 5:Ml(8);M2(10);M3(15);M4(17) | Job5:M1(9);M2(7);M4(8);M2(10);M3(8) |
| Job 6: M2(10);M3(15);M4(8);Ml(15 |  |
| JobSet-5 | JobSet-6 |
| Job 1: Ml(6);M2(12);M4(9) | Job 1: M1(9); M2(11); M4(7) |
| Job 2: M1(18);M3(6); M2(15) | Job 2: Ml(19); M2(20); M4(13) |
| Job 3: M3(9);M4(3);Ml(12) | Job 3: M2(14); M3(20); M4(9) |
| Job 4: M4(6);M2(15) | Job 4: M2(14); M3(20); M4(9) |
| Job 5: M3(3); $\mathrm{Ml}(9)$ | Job 5: M1(11); M3(16); M4(8) |
|  | Job 6: Ml(10); M3(12); M4(10) |


| JobSet-7 | JobSet-8 |
| :--- | :--- |
| Job 1: Ml(6); M4(6) | Job 1: M2(12); M3(21);M4(11) |
| Job 2: M2(11); M4(9) | Job 2: M2(12); M3(21);M4(11) |
| Job 3: M2(9); M4(7) | Job 3: M2(12); M3(21);M4(11) |
| Job 4: M3(16); M4(7) | Job 4: M2(12); M3(21);M4(11) |
| Job 5: Ml(9); M3(18) | Job 5: Ml(10); M2(14);M3(18);M4(9) |
| Job 6: M2(13); M3(19); M4(6) |  |
| Job 7: Ml(10); M2(9); M3(13) |  |
| Job 8: Ml(11); M2(9); M4(8) | JobSet10);M2(14); M3(18);M4(9) |
| JobSet-9 | Job1:Ml(11);M3(19);M2(16);M4(13) |
| Job 1: M3(9);Ml(12);M2(9);M4(6) | Job2: M2(21);M3(16); M4(14) |
| Job 2: M3(16);M2(11); M4(9) | Job3:M3(8); M2(10); Ml(14); M4(9) |
| Job 3: Ml(21); M2(18); M4(7) | Job4: M2(13); M3(20); M4(10) |
| Job 4: M2(20); M3(22); M4(11) | Job5: Ml(9); M3(16); M4(18); |
| Job 5:M3(14);Ml(16);M2(13); M4(9) | Job6:M2(19);M1(21); M3(11);M4(15) |

