FLOWER POLLINATION ALGORITHM FOR MULTI LEVEL LOT SIZING OPTIMIZATION

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Abstract: In this competitive and constantly changing world, meeting the customer requirements within less time by providing less cost is extremely tricky task. This is only possible by optimizing all the different parameters in its life cycle. Here Optimizing the inventory plays a major role.Maintaining the exact amount of inventory, at proper place, in appropriate level is a challenging task for production managers. When we work on Multi level environments this problem becomes even more complex.So, to optimize this kind of problems we applied binary form of Flower Pollination algorithm to solve this complex problem. we solved different inventory lot sizing problems with this FP algorithm and compared the results with genetic algorithm and other algorithms. In all the scenarios our simulation results shown that FP algorithm is better than other algorithms.

1. Introduction

Proper management of inventory is essential for any industry. It acts as the link between production and distribution. If it is not maintained properly it will become a white elephant. If inventory costs increase it shows the direct reflection in product pricing. Hence to optimize the cost basic MRP is not sufficient because its target is to only provide the right number of items to full fill the production requirements in the stipulated time without any deficiency. But in this competitive era with the items having complex product structures cost plays a very important role. One needs to produce the product with less cost to survive in this high competition. So we need to come up with a lot sizing plan which not only satisfies the basic MRP requirement, but also gives us the optimum cost .Here inventory Lot sizing plays a vital role in optimizing the total variable cost which is the sum of holding cost (HC) of inventory and ordering cost (OC) of inventory.

Optimal heuristic and meta heuristic algorithm procedures exists for this problem, but most of them were proven to reach the optimum only in case of single level problems. In ML problems most of these techniques can solve the problem in reasonable time only in case of small instances. But when we work on ML environment with a greater number of levels and multiple sub items, long planning horizons the problem becomes very complex. When we work on real of industrial problems where there are thousands of items there optimizing the cost in reasonable computational time is a really challenging task.

So many heuristics techniques like were used to solve these ML problems .In those one technique is by modifying economic order quantity technique of single level to all the levels of the product structure[1] .The other technique part period balancing defined is by using look head and back strategy[2].one more technique called silver meal heuristic was developed to solve these ML problems by calculating the average costs per period,not only these techniques many other techniques were developed to solve this ML problem. But later researchers started using meta heuristic evolutionary techniques to solve these complex NP hard ML problems[3]. because of their efficient optimization strategies and reasonable computation time these meta heuristic evolutionary techniques took precedence over any other technique.

In early 2000s researchers used genetic algorithms to solve these ML lot sizing issues and gave very good results in terms of solution values for small size problems with limited number of sub items. Later with the success of GA technique many other evolutionary techniques like ant colony (AC), tabu search (TS), simulatedannealing(SA)etc. were developed for theses NP hard problems[4-10]. In recent literature harmonic search (HS) algorithm,Invasive weed (IW) techniques were developed for solving these problems[. Most of these recent techniques were successful in implementation of complex ML, NP hard problems[10-18].But still there is a lot scope and requirement in find the optimal solution in with high computational efficiency.

Here in this research paper our we presented a binary flower pollination algorithm to solve ML assembly structure. This algorithm is tested for feasibility, effectiveness, and computational efficiency. As this algorithm provided the best results, we planned to extend this work to a real-life bus

manufacturing application which is having thousands of sub items and many BOM levels.

This paper is organized as follows: section2 is about presentation of mathematical formulation of ML lot sizing problem.Section 3 is to present binary FP algorithm encoding, framework and pseudo code. Section 4 is about experimental works and resultsand finally section 5 is conclusion.

2. Mathematical Formulation:

In production systems main/final product made up of different sub parts which are raw materials or purchased parts .To satisfy the final product external demand which is generated from the customer requirements we have to make sure that all the sub components are available possibly at lowcost.

BOM generally represents ,different components information of an assembly structure. In the Acyclic representation of BOM ,nodes gives the information about the item/subitem.Edge(k,r) between nodes k,r exist when item k is required to assemble r.GenerallyΓ^{-1}(k),Γ(k) representation is used to represent immediate predecessors &immediatesuccessors.In BOM structure final component is always at the lowest level.If the levels are from 1 to n, n is mostly a purchased part.

In the mathematical formulation of ML lot sizing problem, we have to find out the final lot sizes of final product as well as all sub parts. So there are different objectives and constraints that needs to be considered while formulating such problem. Following are the considerations to formulate the problem

- No backordering is allowed.
- Components are not allowed to sell outside. So, independent demand exists only for final product .Remaining all items are having dependent demands.
- Lead times are assumed as zero.
- No schedule receipts, no initial inventories.so net and gross requirements are same.
- No variable cost /purchase parameters were taken into consideration.

Table 1

ML lot sizing problem notations

Parameters related to cost : $s_{k,pt}$ $h_{k,pt}$	'k' item set up cost in period 'pt' 'k' item holding cost in period 'pt'
Parameters related to quantity $d_{k,pt}$ $q_{k,pt}$	Gross requirement of item 'k' in period 'pt' Quantity of item 'k' delivered in the beginning of period 'pt'

$I_{k,pt}$ $b_{k,pt}$	Inventory level of item 'k' required at the end of period 'pt' Boolean variable to take decision wheather order is placed or not
Technical information l_k $c_{k,r}$	Lead time for item k Quantity of item k required to produce unit of item r

For problem formulation we followed the references [1] and then modified according to our ML assembly structure requirement.

$$Minimize \sum_{k=1}^{n} \sum_{pt=1}^{T} s_{k,pt}\, b_{k,pt} + h_{k,pt} I_{k,pt} \qquad (1)$$

$$I_{k,pt} = I_{k,pt-1} + q_{k,pt} - d_{k,pt} \qquad (2)$$

$$d_{i,kt} = \sum_{r\epsilon\Gamma(k)}^{d_{i,kt}} q_{r,pt+lr}\, c_{k,r} \qquad (3)$$

$$q_{k,pt} - Mb_{k,pt} \le 0 \quad b_{k,pt}\epsilon\{0,1\} \qquad (4)$$

$$I_{k,pt} \ge 0 \qquad (5)$$

$$q_{k,pt} \ge 0 \qquad (6)$$

The Objective function shown in equation (1) is the minimization of sum of HC and SC of all the items in the given planning horizon.Equation(2) represents the inventory level at the end of given period.Equation(3) make sure that no items is sold outside customer .Equation(4) tells about the setup cost is applied when a lot is purchased.Equation(5) tells that backlogging of inventory is not allowed &(6) make sure that production is always positive /0.

3.Flower pollination algorithm:

Pollination is a fascinating phenomenon in the nature. Inspired from its evolutionary characteristics FPA algorithm was developed in 2012 by Xin-She Yang.This algorithm characteristics are defined from the inspiration of reproduction in flowering plants.The biological reproduction process

characteristics are defined in FPA algorithms by following 4 governing rules[19]

1.   Biotic pollination & cross pollination was done by the biotic pollinators like insects /birds performing lévyflights.

2.   Abiotic /self pollination uses abiotic non-living methods such as wind to carryout pollination which is called as local pollination.

3.   Flower constancy can be considered as the reproduction probability is proportional to the similarity of two flowers involved.

4.   Global or local pollination can be controlled by probability parameter p.

In our algorithm we are mapping the natural process of pollination to FPA. In reality each flower contains millions of pollen grains. But for the simplification purpose we assume each flower is containing one pollen gamete. So one solution typically represents plant/flower/pollen gamete.

FPA algorithm mainly contains 2 steps ,in that one is replated to global pollination and the other is related to local pollination .

Global pollination of flowering plant with respect to the algorithm was represented as follows.

$$x_i^{t+1} = x_i^t + L(x_i^t - gb)$$

Here gb represents global best and x_i^t represents solution vector x_i in iteration 't'. Here x_i^{t+1} is modified x_i in the next iteration 't+1'.Here L represents insects pollination strength.Insects move different lengths by carrying pollen gametes, which is controlled by Lévy flights taken from lévy distribution.

$$L = \frac{\lambda \Gamma(\lambda) \sin\left(\frac{\lambda\Pi}{2}\right)}{\Pi} \frac{1}{s^{1+\lambda}} \quad (s \gg s_0 > 0)$$

$$s = \frac{U}{|V|^{1/\beta}}, \quad U \sim N(0, \sigma^2) \quad \text{and} \quad V \sim N(0,1).$$

Here $U \sim N(0, \sigma^2)$ denotes that the samples have been drawn from a Gaussian normal distribution with variance of σ^2 and zero mean. For the purpose of calculation of variance one can use the formula:

$$\sigma^2 = \left\{ \frac{\Gamma(1+\beta)}{\beta \Gamma\frac{1+\beta}{2}} \frac{\sin\left(\frac{\pi\beta}{2}\right)}{2^{\frac{\beta-1}{2}}} \right\}^{1/\beta}.$$

Here constant   λ is used to create lévynumbers.andhere s represents step length and this algorithm is for large step lengths.

Local pollination of the flowers are represented by the following equation

$$x_i^{t+1} = x_i^t + \epsilon(x_j^t - x_k^t)$$

Here x_j^t and x_k^t are the pollen grains from different flowers /solutions in the neighbourhood of solution i. Here ϵ represents the local walk of abiotic pollination, which is calculated from [0,1] uniform distribution.

Here to convert the solution values to the binary form sigmoid function is used

$$S(x_i^p) = \frac{1}{1 + e^{x_i^p}}$$

$$x_i^t = \begin{cases} 1 & S(x_i^p) > \sigma \\ 0 & otherwise \end{cases}$$

Here σ value comes from uniform distribution U[0,1].

4.Experiments and their simulation results :

Here we have presented various example problems from the literature to test our FPA algorithm behaviour. To conduct all these simulation experiments authors used MATLAB software.PC specifications are 8GB ram and 2.8 GHZ CPU.All the simulations were performed for 100 times to findout the results

Here 3 different product structures were used with7 different planning horizons.Following are the different problems considered for the Experiments

1.7×6 problem [20] represents problem with 6 items BOM structure with 6 periods planning horizon.

2. 6×10,6×12,6×15 problems [21]here 6 items problem with different planning horizons were considered to compare the simulation results.

3.9×10,9×12,9×15 problems [21] here 9 items problem with different planning horizons were considered to compare the simulation results.

In all the cases FPA was applied and and simulation results of optimum value and computational time were compared with other algorithms.

The following are the simulation results of 7×6 problem and the figure clearly shows the dominance of the FPA algorithm over other evolutionary algorithms like GA ,SA,TS,LR.

Size of the Problem	Algorithm type	Optimum cost value	Simulation time to reach optimum(sec)
	FPA	8320	<0.2

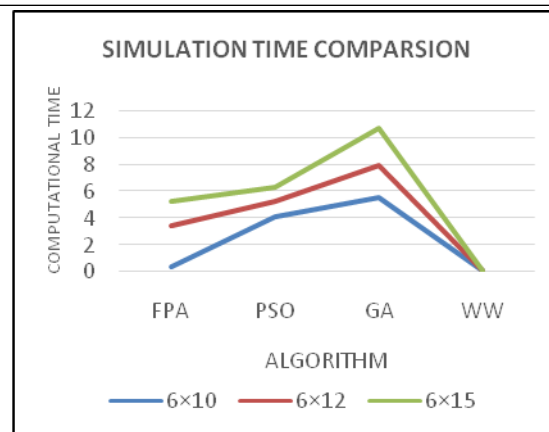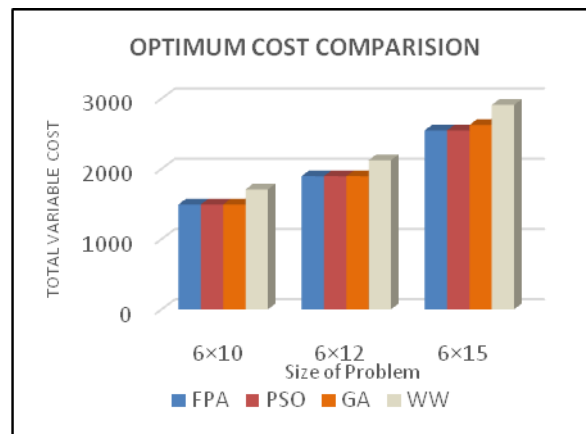|	GA	9245	10.10
7items×6periods	SA	10740	9.90
	TS	9620	8.80
	LR	9239	34.10
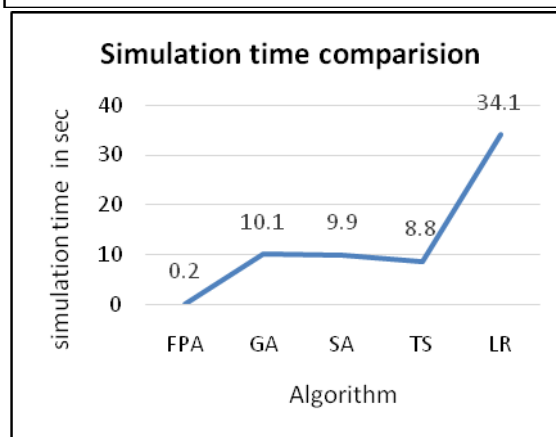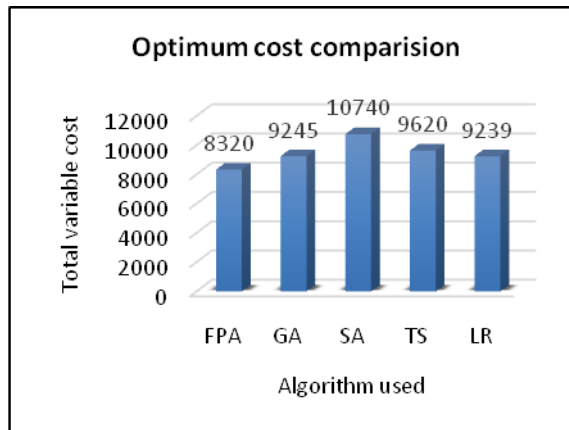
The following are the simulation results of 6×10,6×12,6×15 problems and the following figure clearly shows the dominance of the FPA algorithm over other evolutionary algorithms like PSO ,GA,WW.

Table 8

Computational Results of MLLSOP with 6 items and different planning horizons

Size of Problem	Algorithm	Optimum cost	Time to find out Optimum solution(s)
6items×10periods	FPA	1493	0.4
	PSO	1493	4.2
	GA	1493	5.6
	WW	1707	<0.1
6items×12periods	FPA	1895	3.5
	PSO	1895	5.3
	GA	1895	8.0

	WW	2123	<0.1
	FPA	2546	5.3
6items×15periods	PSO	2546	6.3
	GA	2623	10.7
	WW	2909	<0.1

The following are the simulation results of 9×10,9×12,9×15 problems and the following figure clearly shows the dominance of the FPA algorithm over other evolutionary algorithms like PSO ,GA,WW.

Size of Problem	Algorithm	Optimum cost	Time to find out Optimum solution(s)
	FPA	2043	4.1
	PSO	2043	6.5
9items×10periods	GA	2043	10.1
	WW	2807	<0.1
	FPA	2522	5.7
	PSO	2522	7.2
9items×12periods	GA	2522	12.9

	WW	3498	<0.1
	FPA	3448	8.5
	PSO	3448	9.2
9items×15periods	GA	3714	16.3
	WW	4834	<0.1

➤

➤ WW algorithm is quicker than FPA because it is a single pass method which is failed in finding the optimum solution.
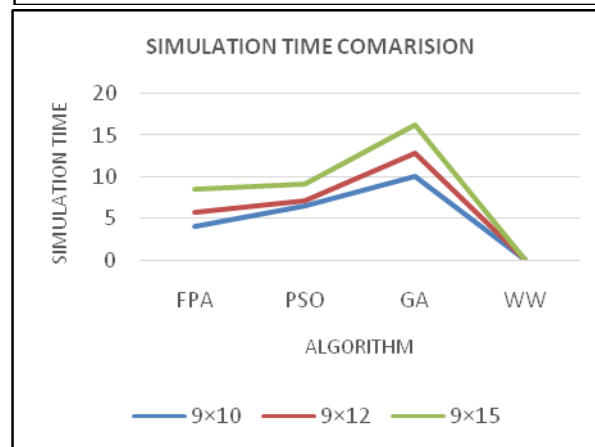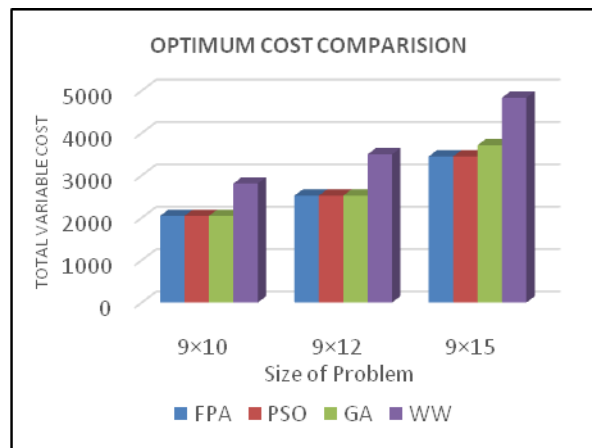
Conclusion:

Solving Multi level Lot sizing issues in manufacturing is one of the key issues of inventory control. The necessity of optimizing the cost in minimum time is very important in this era of rapidly changing environments. In these days of artificial intelligence and machine learning optimization of costs in very quick time is really an important concern.

➤ Flower pollination algorithm was implemented for the inventory lot sizing problem with multiple levels

➤ FPA algorithm outperformed all the other method solutions and successful in finding the optimum cost in reasonable amount of time .

➤ It is efficient in terms of computational time aspect as well when compared with other evolutionary methods.

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